



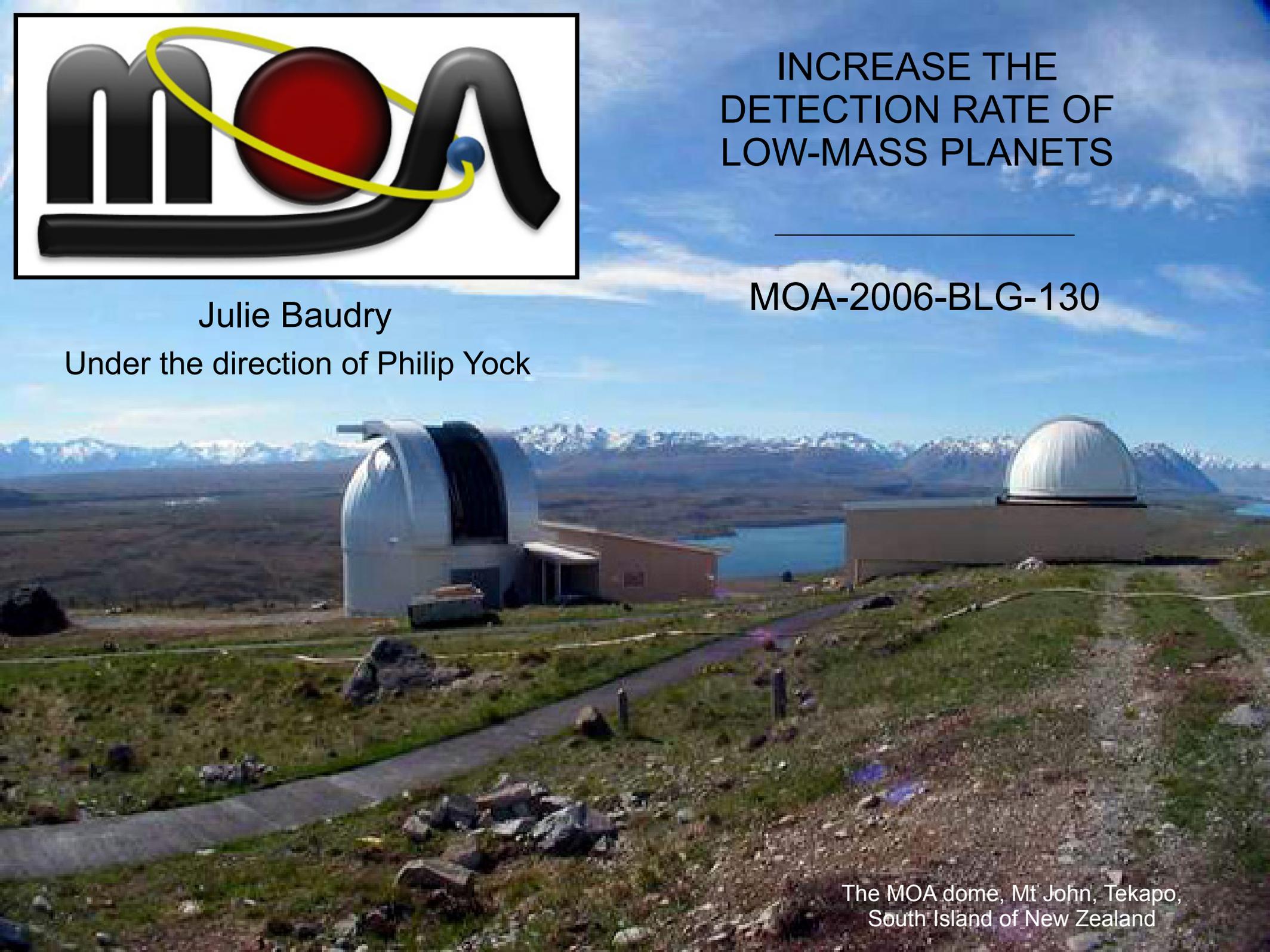
Julie Baudry

Under the direction of Philip Yock

# INCREASE THE DETECTION RATE OF LOW-MASS PLANETS

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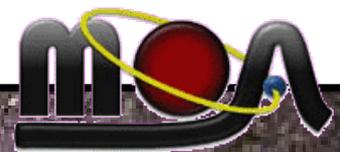
MOA-2006-BLG-130



The MOA dome, Mt John, Tekapo,  
South Island of New Zealand

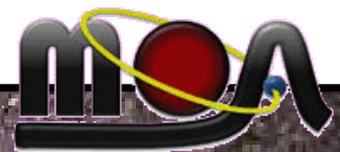
# SUMMARY

- Introduction



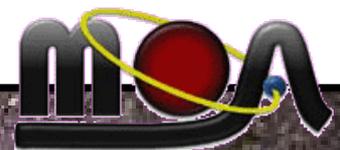
# SUMMARY

- Introduction
- Planetary perturbation and magnification

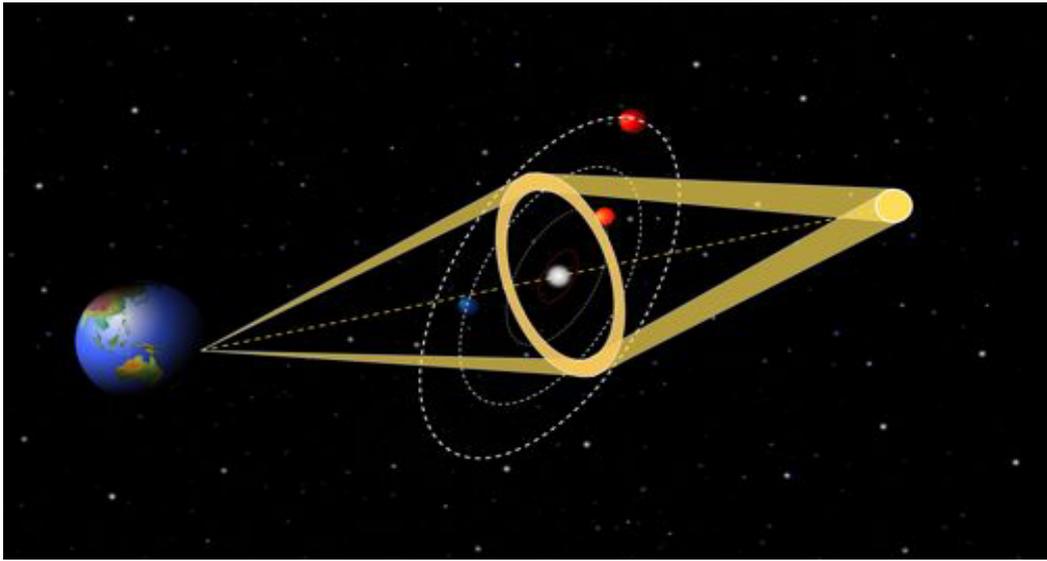


# SUMMARY

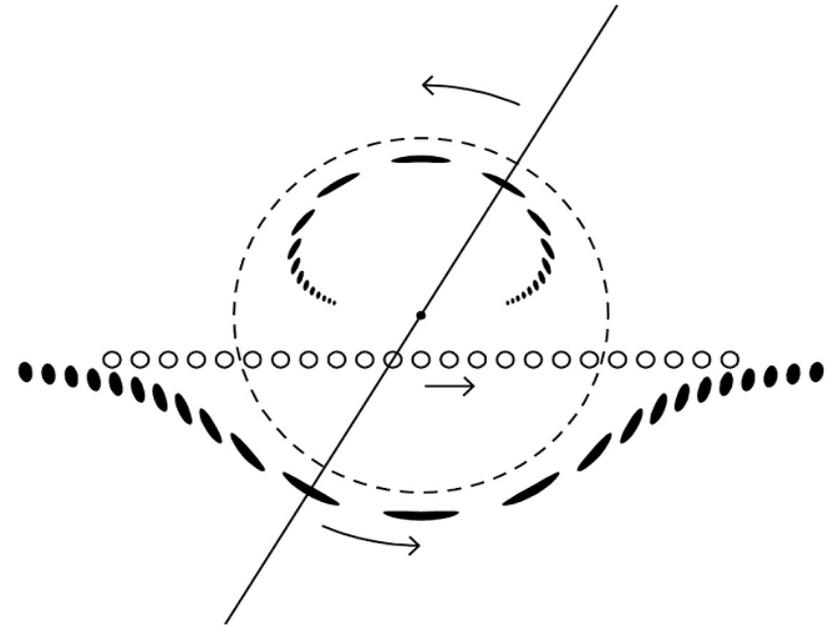
- Introduction
- Planetary perturbation and magnification
- MOA – 2006 – BLG – 130



# I – Gravitational Microlensing



Light from the source star is bent into an Einstein ring around the lens star



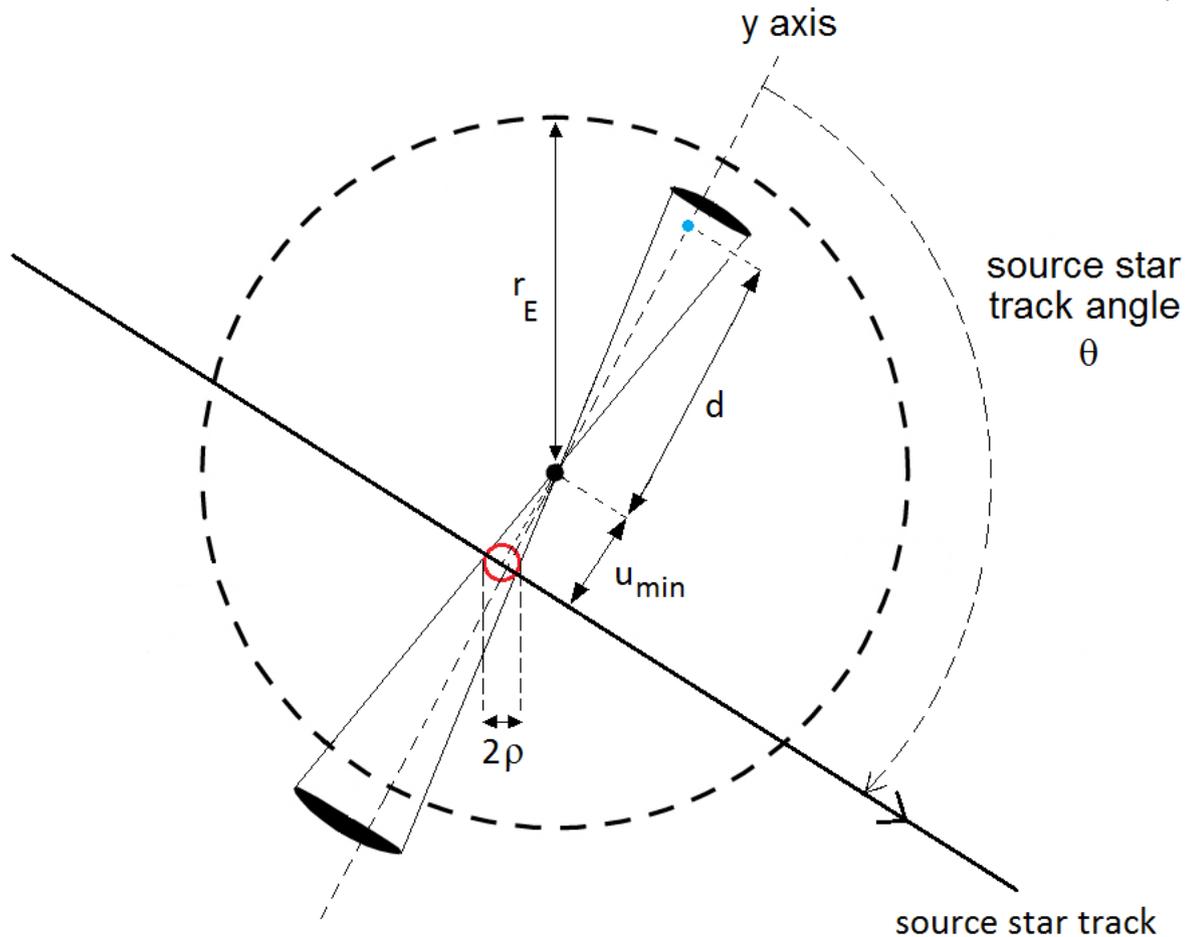
Bohdan Paczynski, *Ann. Rev. Astron. Astrophys.* 34, 419 (1996)

$$r_E = \left( \frac{4 G M_l}{c^2} \cdot \frac{D_l (D_l - D_s)}{D_s} \right)^{1/2}$$



## II – Planetary perturbation and magnification

### Binary lens configuration



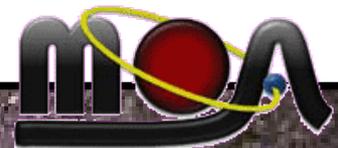
### Planet parameters:

- $q$  = mass ratio (planet / lens)
- $d$  = distance lens – planet
- angle from the y axis is fixed at 0

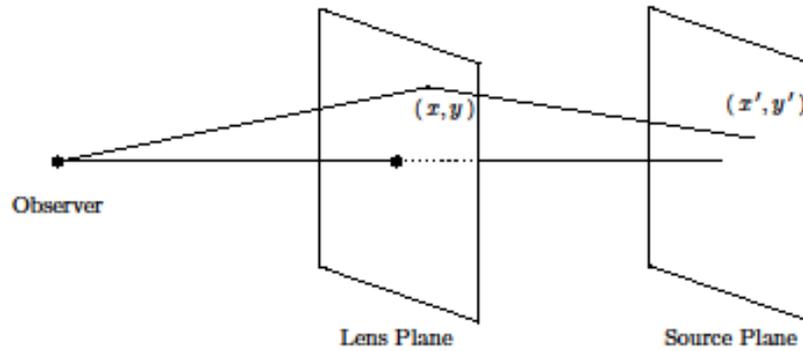
### Track parameters:

- $u_{\min}$  = minimum impact parameter
- $\rho$  = source star radius
- $\theta$  = source track angle
- the time to cross the Einstein ring and the time of minimum impact are chosen randomly, in the range of real events
- no parallax

(All distances are given in unit of  $r_E$ )



## II – Planetary perturbation and magnification



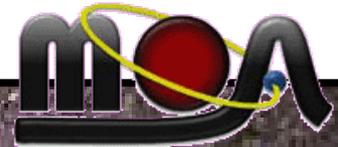
✓ Magnification maps are computed for 9 systems [lens + planet] using the inverse ray shooting technique

⇒ fractional maps

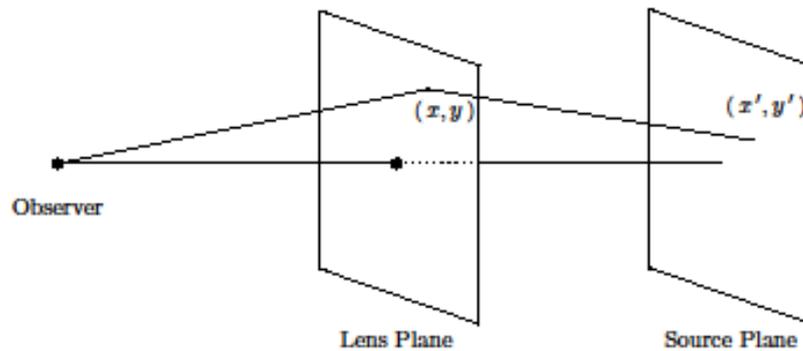
$$x' = x - \frac{m_1 x}{x^2 + y^2} - \sum_{i=1}^n \frac{m_i (x - x_i)}{(x - x_i)^2 + (y - y_i)^2},$$
$$y' = y - \frac{m_1 y}{x^2 + y^2} - \sum_{i=1}^n \frac{m_i (y - y_i)}{(x - x_i)^2 + (y - y_i)^2}.$$

Creating theoretical microlensing lightcurves from magnification maps, L. Philpott, 2005

·Lydia Philpott, 2005; C.S. Botzler, 2006; Sarah Holderness, 2008; Yvette Perrott, 2009.



## II – Planetary perturbation and magnification



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Creating theoretical microlensing lightcurves from magnification maps, L. Philpott, 2005

✓ Magnification maps are computed for 9 systems [lens + planet] using the inverse ray shooting technique

⇒ fractionnal maps

✓ Theoretical light curves

⇒ No parallax

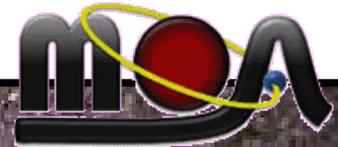
⇒ Source track angle :  $\theta = 0$

⇒ for each system, 3 values of the source star radius are tested

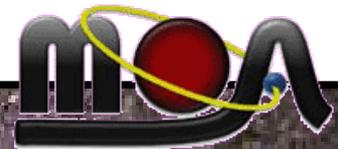
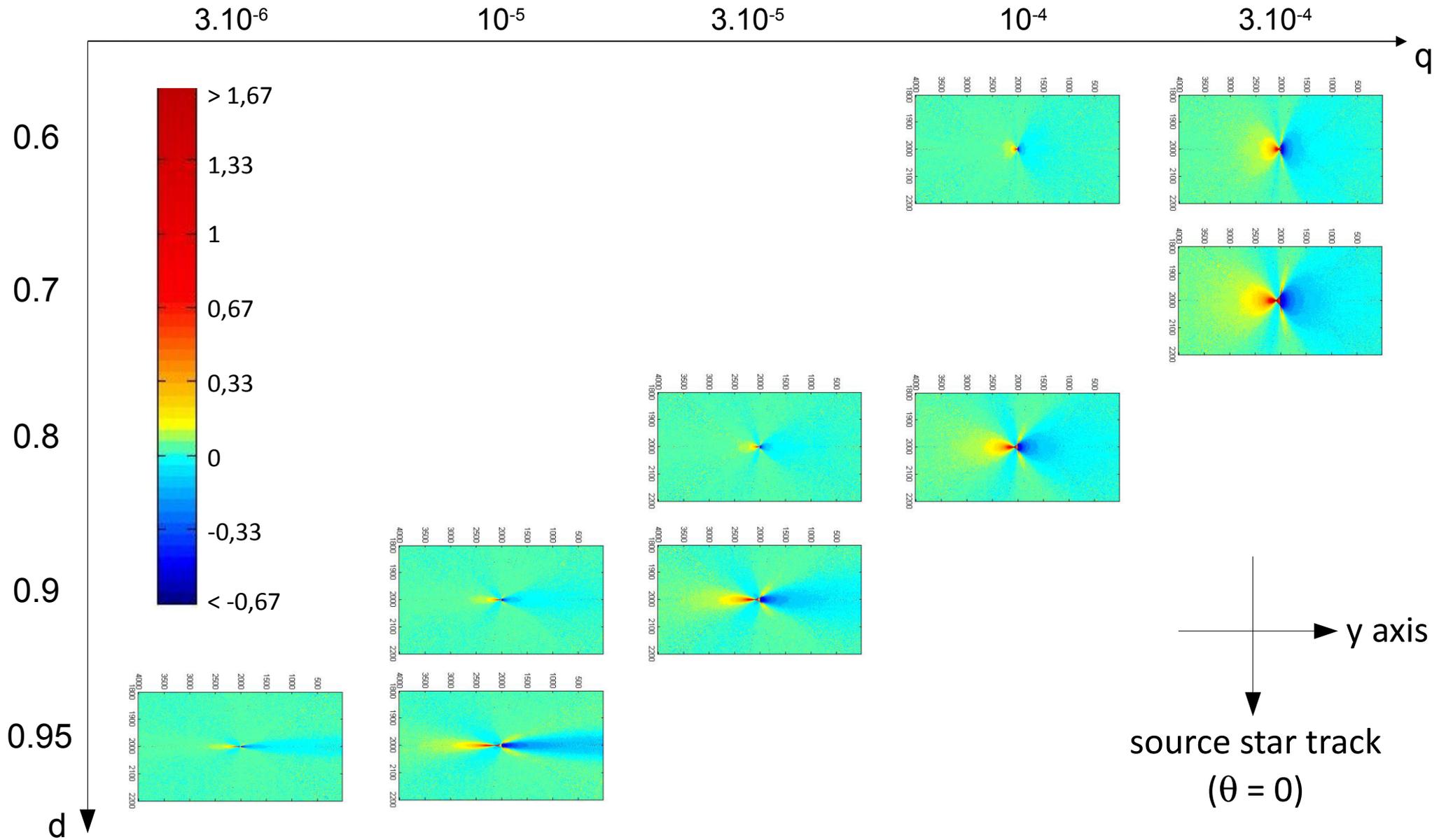
$$\rho = \{0,001; 0,002 ; 0,005\}$$

⇒ 13 values of  $u_{\min}$  are have been simulated, in a range of  $|u_{\min}| \in [0 ; 0,03]$

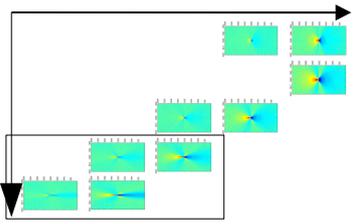
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## II – Planetary perturbation and magnification

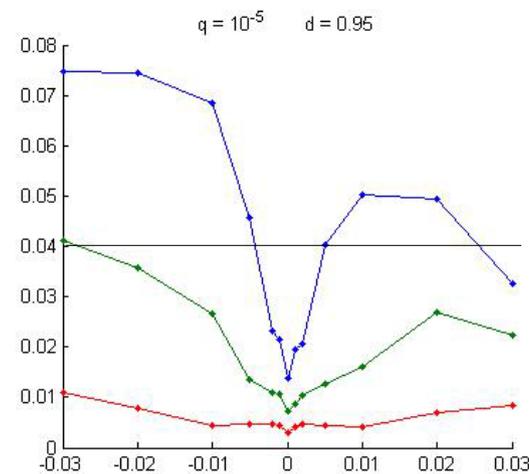
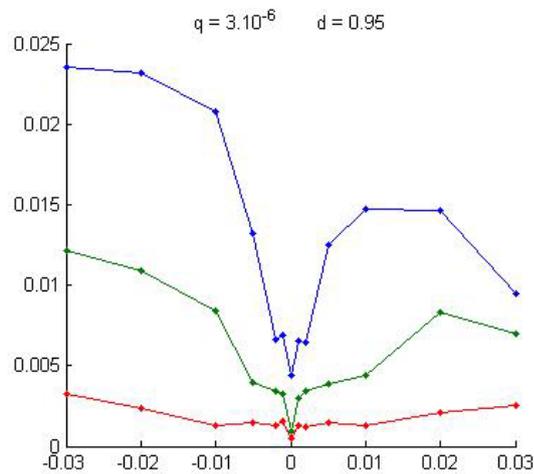
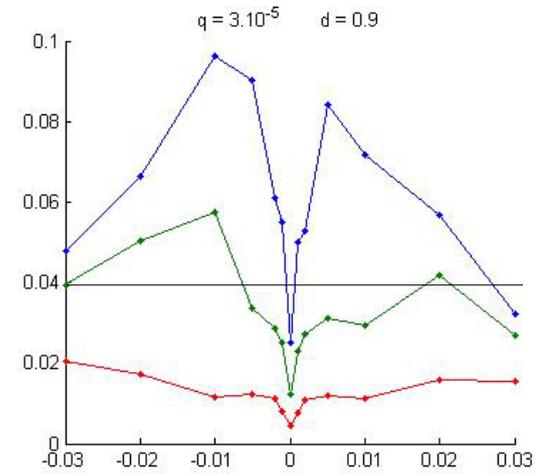
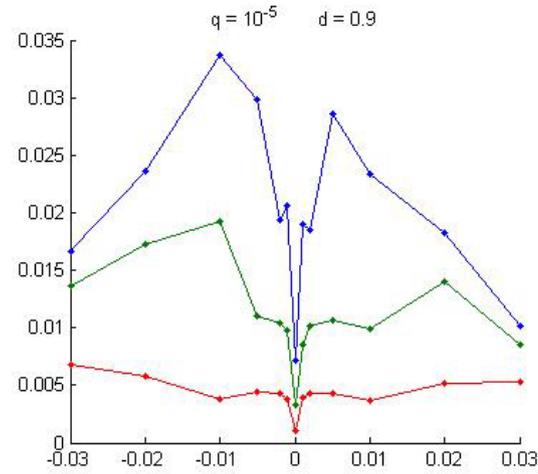


## II – Planetary perturbation and magnification



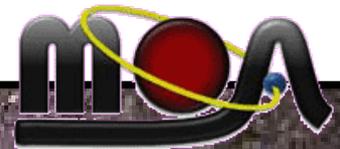
detectability threshold  $\sim 4\%$

- $\rho = 0.005$
- $\rho = 0.002$
- $\rho = 0.001$

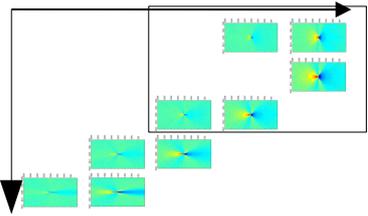


% of deviation to the light curve

$u_{\min}$



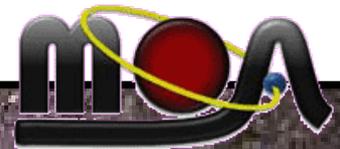
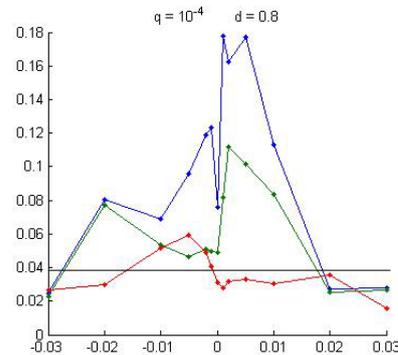
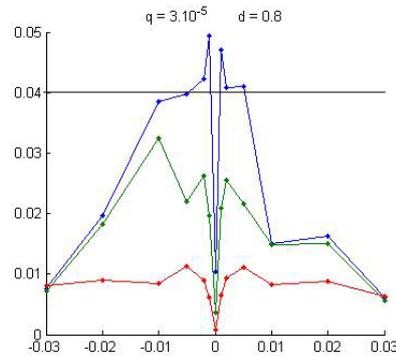
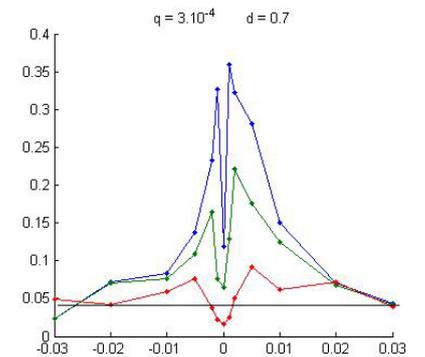
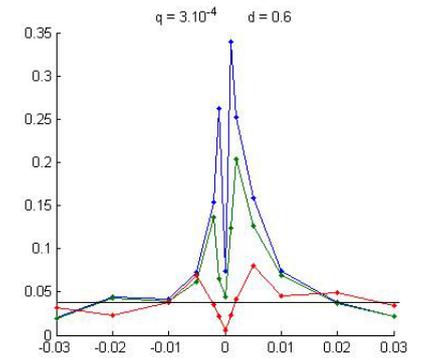
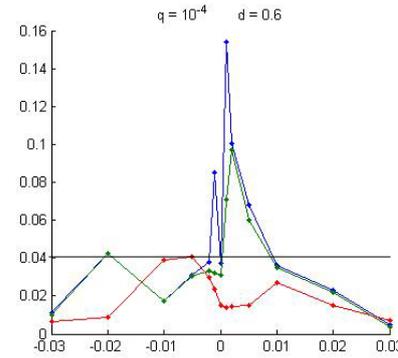
## II – Planetary perturbation and magnification



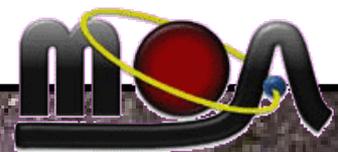
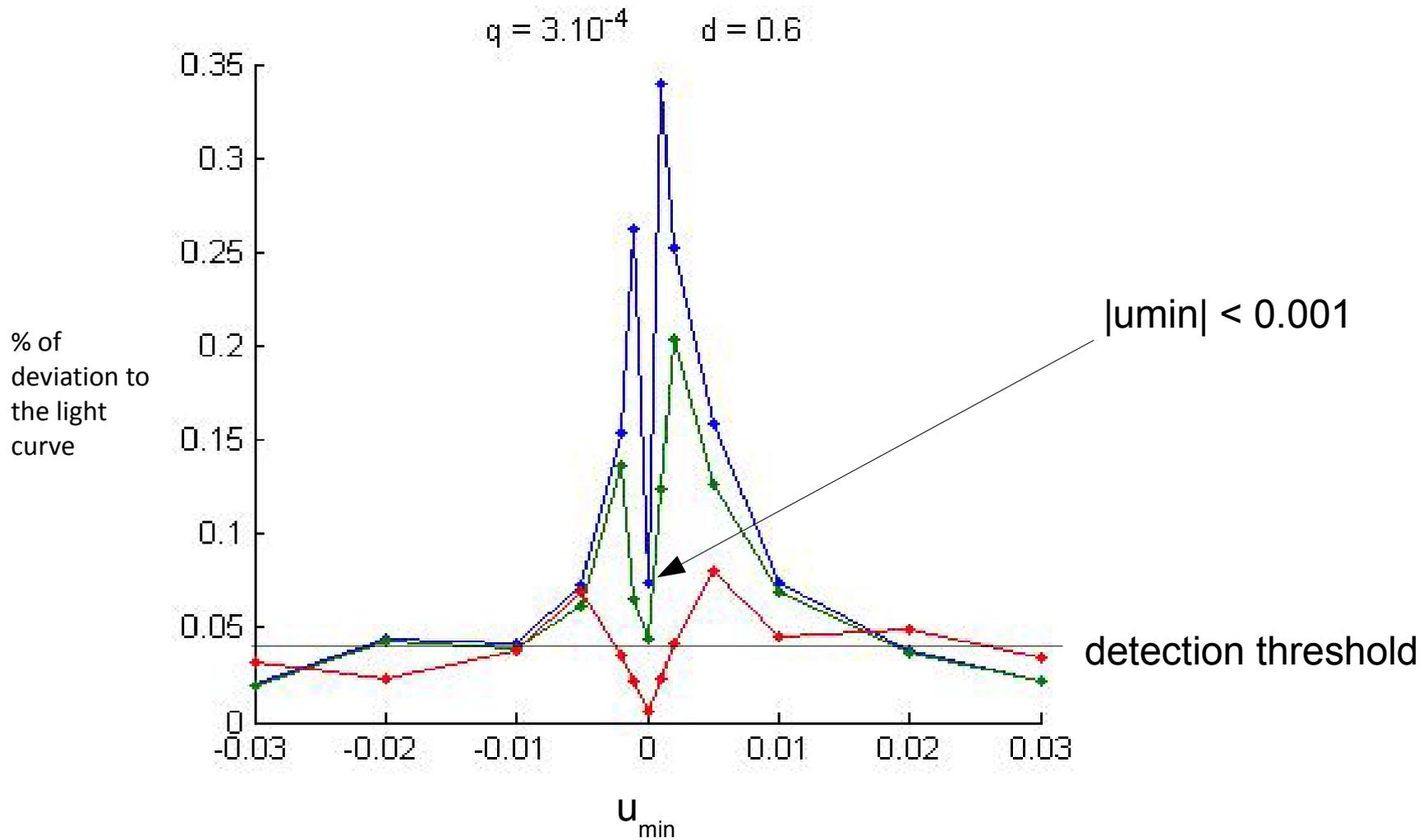
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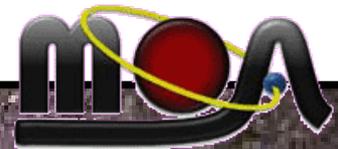
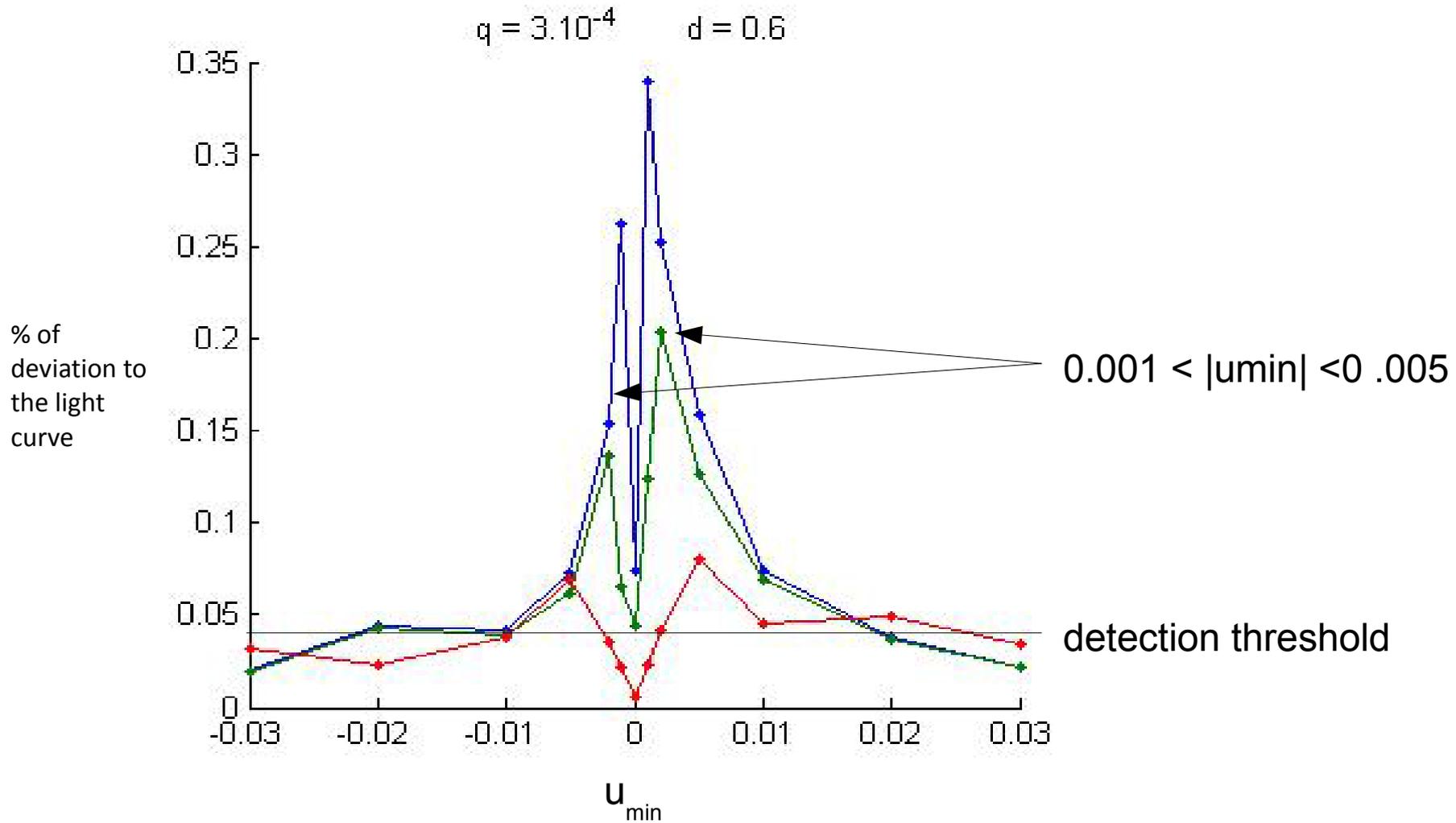
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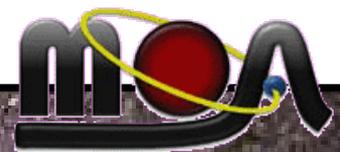
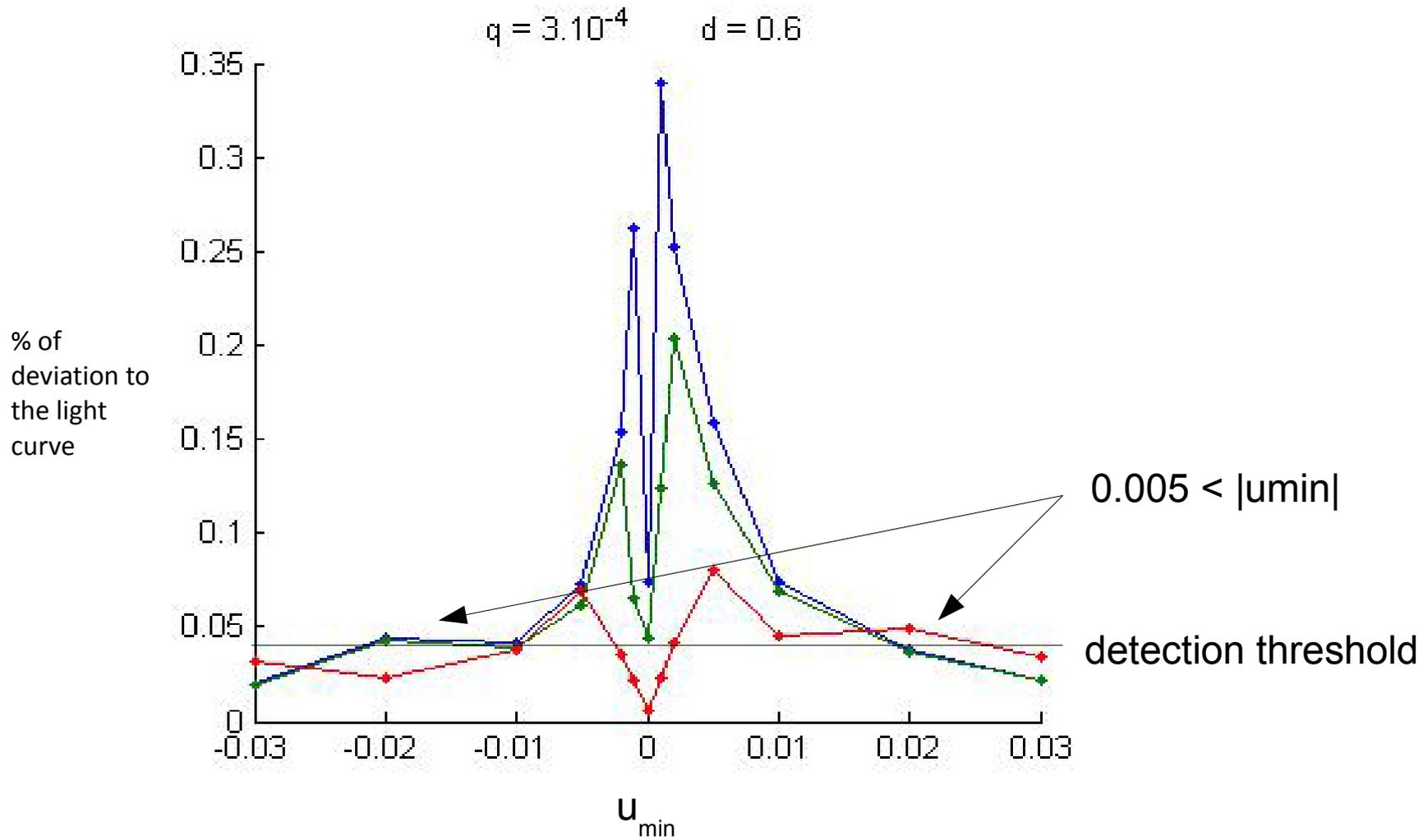
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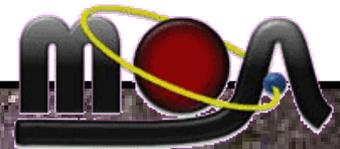
## II – Planetary perturbation and magnification



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→ We can distinguish 3 zones:

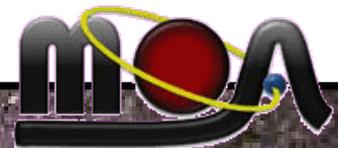
|  | I | II | III |
|--|---|----|-----|
| Geometry                                   |   |    |     |
| Range of $u_{\min}$                        |   |    |     |
| Consequences on the planetary perturbation |   |    |     |



## II – Planetary perturbation and magnification

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|   | I  | II | III |
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| <b>Geometry</b>                                   | The source transits the lens                             |    |     |
| <b>Range of <math>u_{\min}</math></b>             | $u_{\min} < \rho$  |    |     |
| <b>Consequences on the planetary perturbation</b> | Low mass planets with $q < 3 \cdot 10^{-5}$ undetectable |    |     |



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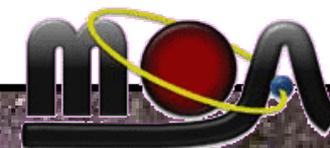
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| <b>Geometry</b>                                   | The source transits the lens                             | The planet is closer to the Einstein ring than the length of an arc.   |     |
| <b>Range of <math>u_{\min}</math></b>             | $u_{\min} < \rho$  | $\rho < u_{\min} < \frac{2\rho}{1-d}$  |     |
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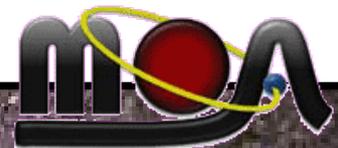
|   | I  | II   | III   |
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| <b>Geometry</b>                                   | The source transits the lens                             | The planet is closer to the Einstein ring than the length of an arc.   | The planet is further away than the length of an arc.                         |
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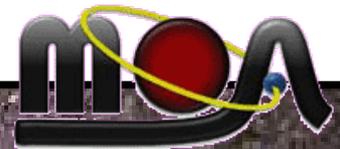
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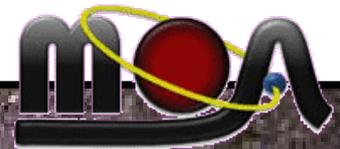
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→ Transit events insensitive to low-mass planets



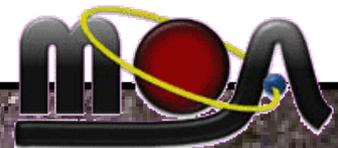
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- Transit events insensitive to low-mass planets
- Moderate magnification events sensitive to low mass planets quite close to the ring
- More events occur at lower magnifications, but larger telescopes are needed to monitor them



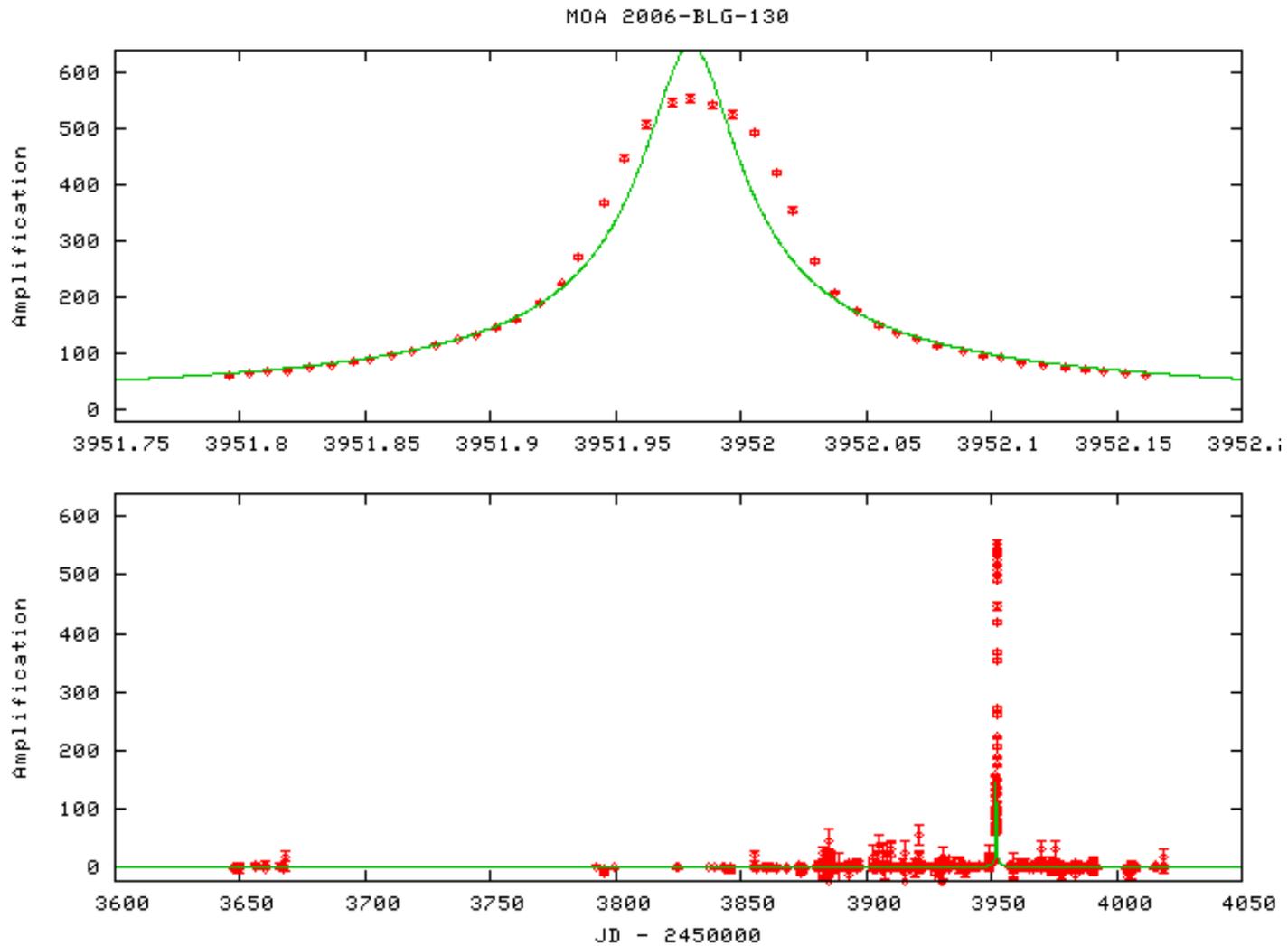
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- Transit events insensitive to low-mass planets
- Moderate magnification events sensitive to low mass planets quite close to the ring
- More events occur at lower magnifications, but larger telescopes are needed to monitor them
- Low mass planets not detectable if they are not close to the ring

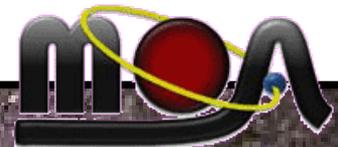


### III – MOA-2006-BLG-130 : event in zone I

#### MOA data



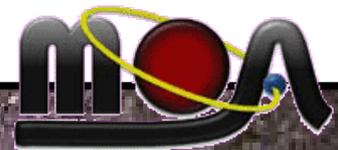
[http://www.phys.canterbury.ac.nz/moa/microlensing\\_alerts.html](http://www.phys.canterbury.ac.nz/moa/microlensing_alerts.html)



✓ Using the same code than previously, magnification maps are computed for 27 couples (q ; d):

$$\begin{cases} q = 10^{-4}, 3 \cdot 10^{-4}, 10^{-3} \\ d = 0.3, 0.5, 0.7, 0.8, 0.85 \end{cases}$$

$$\begin{cases} q = 3 \cdot 10^{-6}, 10^{-5}, 3 \cdot 10^{-5} \\ d = 0.8, 0.85, 0.9, 0.95 \end{cases}$$



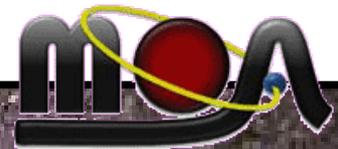
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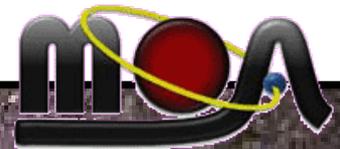
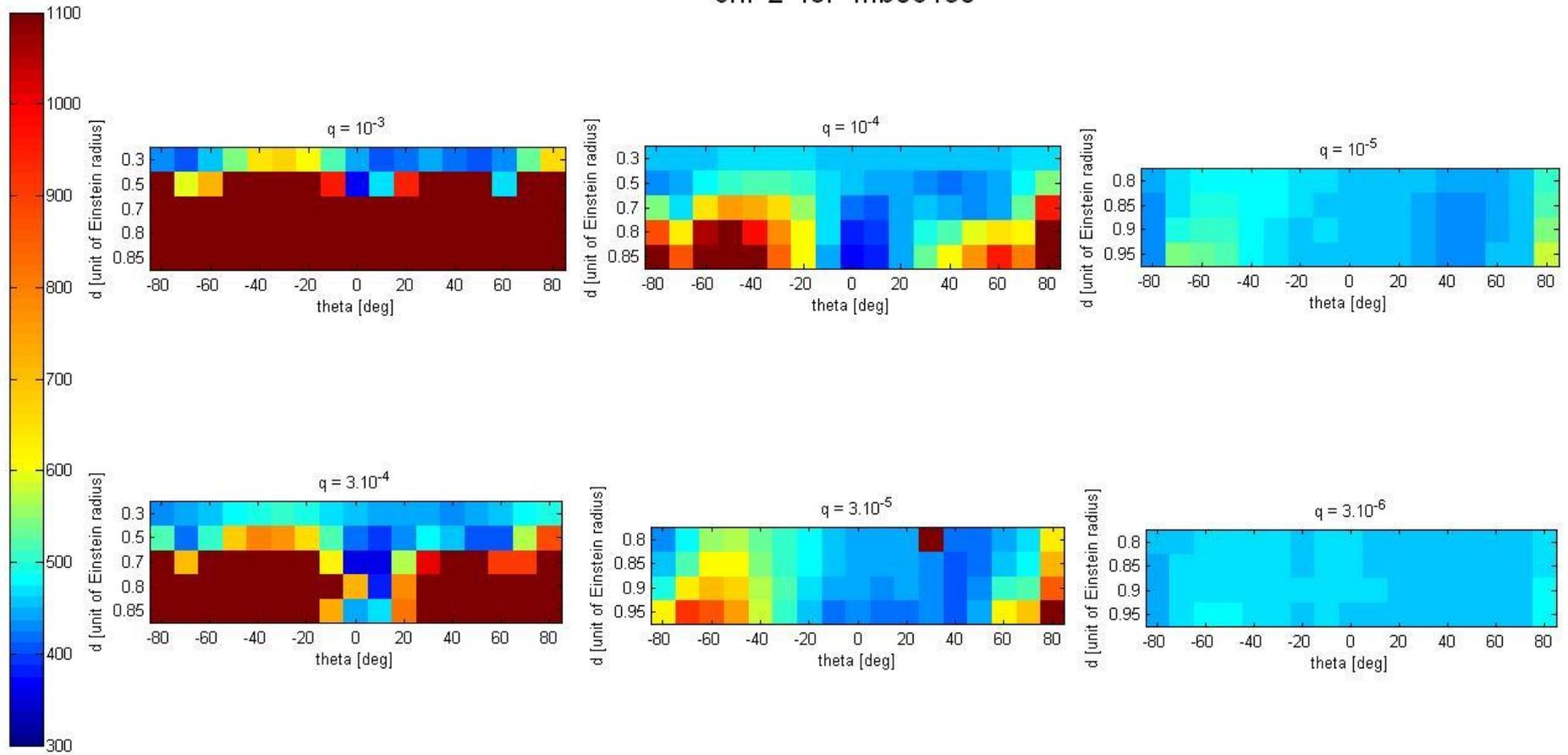
✓ We use a  $\chi^2$  marginalisation method to determine the best model:

- Fixed parameter : source track angle  $\theta$
- No parallax



# III – MOA-2006-BLG-130 : event in zone I

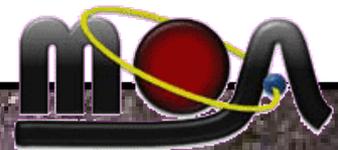
chi<sup>2</sup> for mb06130



### III – MOA-2006-BLG-130 : event in zone I

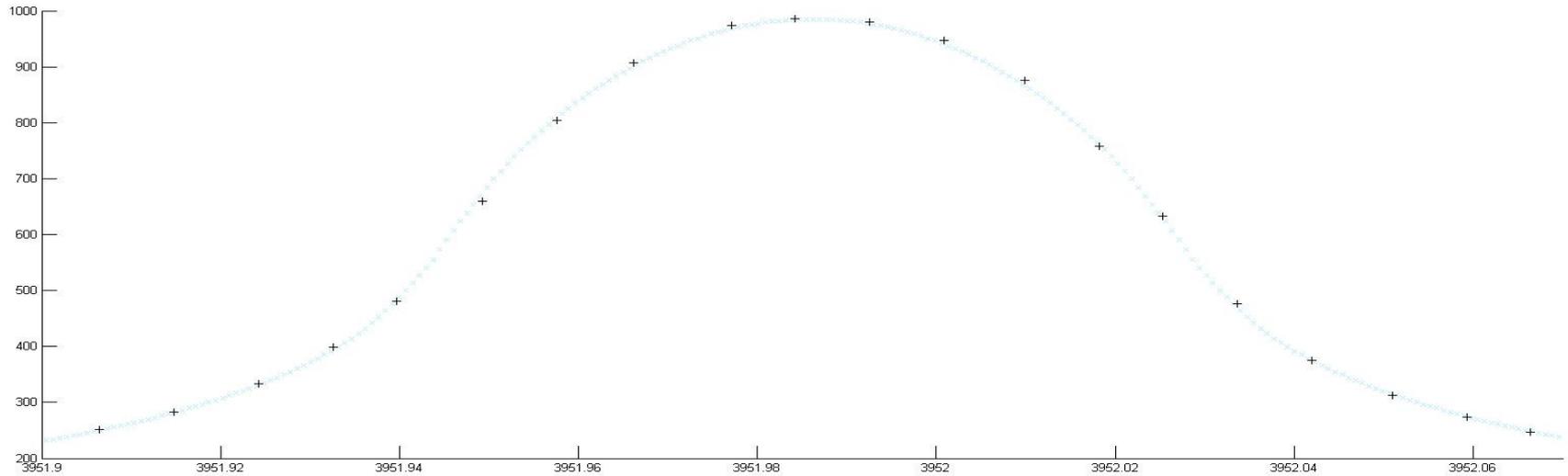
· Best fits and single lens parameters:

| q                 | d    | $\rho$              | $\theta$ | $u_{\min}$           | $t_E$                  | $t_0$              | $\chi^2$ |
|-------------------|------|---------------------|----------|----------------------|------------------------|--------------------|----------|
| $3 \cdot 10^{-4}$ | 0.7  | $0.0022 \pm 0.0001$ | 0        | $0.0002 \pm 0.0001$  | $3951.9862 \pm 0.0002$ | $18.91 \pm 0.005$  | 359.18   |
| $10^{-4}$         | 0.85 | $0.0022 \pm 0.0001$ | 0        | $-0.0001 \pm 0.0001$ | $3951.9862 \pm 0.0002$ | $18.955 \pm 0.005$ | 364.44   |
| 0                 | 0    | $0.0022 \pm 0.0001$ | -        | $-0.0002 \pm 0.0001$ | $3951.9862 \pm 0.0002$ | $19.1 \pm 0.005$   | 464.93   |

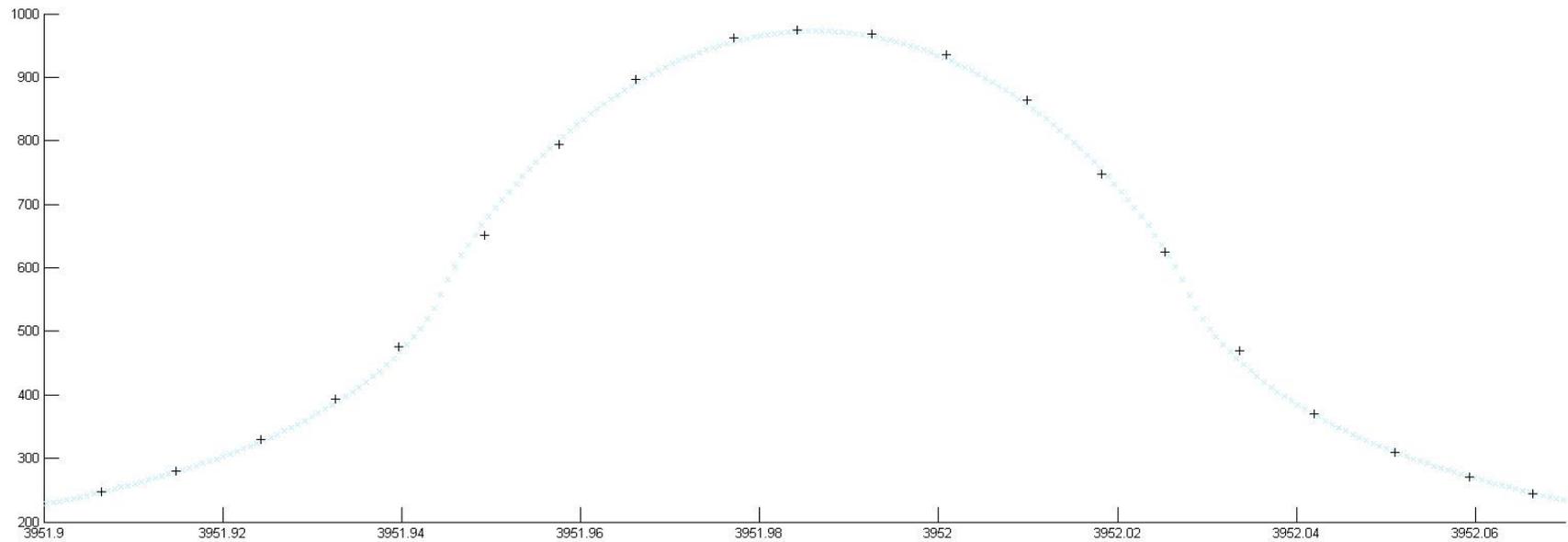


# III – MOA-2006-BLG-130 : event in zone I

$q = 10^{-4}$   
 $d = 0.85$



single lens



JD - 2450000



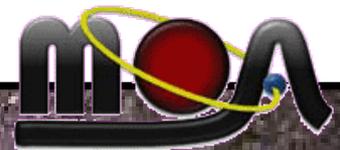
### III – MOA-2006-BLG-130 : event in zone I

→ Finer simulations could be done in zones of lowest  $\chi^2$ .



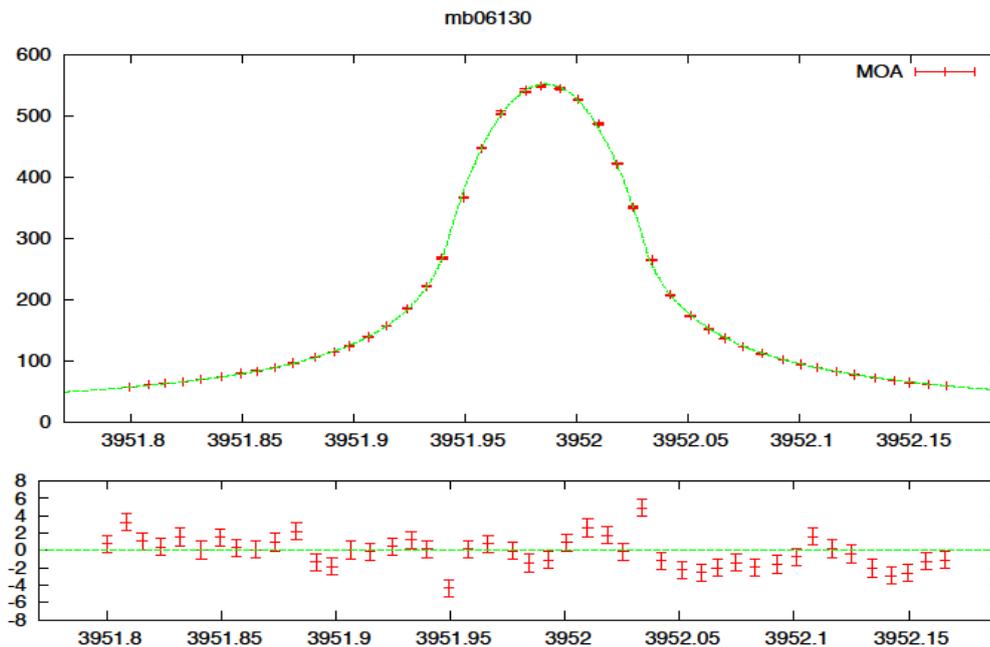
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- Finer simulations could be done in zones of lowest  $\chi^2$ .
- Data are too sparse to be assertive on the presence of a planet.



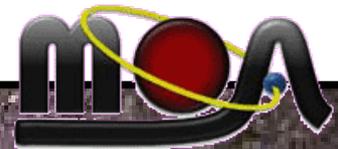
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- Finer simulations could be done in zones of lowest  $\chi^2$ .
- Data are too sparse to be assertive on the presence of a planet.
- Other phenomena could be the cause the deviation to the light curve :



Periodic phenomenon ?

By Ian Bond, University of Auckland, New Zealand



Thanks

Thanks to the Physics Department of the UoA, New Zealand, to the Earth and Sky company and astronomers of the Mt John Observatory.

Very special thanks to Philip Yock.

**AND THANK YOU FOR YOUR ATTENTION!**

